

# Cryptanalysis of Secure and Lightweight Conditional Privacy-Preserving Authentication for Securing Traffic Emergency Messages in VANETs

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**Abstract**—In their paper, Wei et al. proposed a lightweight protocol for conditional privacy-preserving authentication in VANET. The protocol aims to achieve ultra-low transmission delay and efficient system secret key (SSK) updating. Their protocol uses a signature scheme with message recovery to authenticate messages. This scheme provides security against adaptively chosen message attacks. However, our analysis reveals a critical vulnerability in the scheme. It is susceptible to replay attacks, meaning a malicious vehicle can replay a message multiple times at different timestamps. This action undermines the overall effectiveness of conditional privacy. We suggest possible solutions to address these vulnerabilities and enhance the security of VANET communication.

**Index Terms**—VANET, privacy-preserving authentication, universal forgery, replay attack.

## I. INTRODUCTION

VEHICULAR Ad Hoc Networks (VANETs) have been developed to enhance transportation safety and efficiency. However, the wireless channels they use are susceptible to attacks, making it essential to secure VANETs. Privacy is also a significant concern in VANETs, and although Pseudo-identity techniques can address this issue, it is challenging to manage them on resource-constrained vehicles. Conditional privacy-preserving authentication (CPPA) schemes are a promising solution for securing VANETs. However, the computational overhead of bilinear pairing operations is a significant barrier, making developing low-latency solutions for CPPA schemes necessary.

A recent CPPA scheme, developed by Wei et al. [1], aimed to address these challenges. Unfortunately, a recent analysis by Zhang et al. [2] revealed that this scheme is vulnerable to universal forgery. This flaw allows attackers to forge valid signatures on any message, making it possible to disseminate false information undetected. Our analysis also shows that Wei et al. [1] is insecure against replay attacks, which means that a malicious vehicle can replay a message multiple times at different timestamps, undermining the overall effectiveness of conditional privacy. Our analysis highlights the need for robust security mechanisms in VANETs and uncovers the reasons behind these vulnerabilities.

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## II. REVIEWS OF WEI ET AL.'S CONDITIONAL PRIVACY-PRESERVING AUTHENTICATION IN VANET

This section briefly outlines Wei et al.'s CPPA scheme [1]. For comprehensive details, readers are encouraged to refer to the original work [1].

### A. System Setup Phase

In this phase, a trusted authority (TA) generates an elliptic curve group  $G$  over a finite field  $F_p$ , where  $p$  is a large prime, and selects a generator  $P$ . TA then randomly chooses a system secret key (SSK)  $s \in \mathbb{Z}_q$  and computes its public key  $P_{pub} = -sP$ . Each vehicle  $V_i$  registers with TA by providing its identity  $I_{Di}$  and password  $PW_i$ . TA implants the SSK  $s$  into the tamper-proof device (TPD) of vehicle  $V_i$ . Finally, TA publishes the system public parameters  $Para = (G, P, P_{pub}, q, H_1, H_2, H_3, H_4, H_5)$  in VANET.

### B. Signature Generation

During signature generation, vehicle performs the following steps:

- First, the vehicle  $V_i$  inputs its identity  $I_{Di}$  and password  $PW_i$  into TPD to verify the legality of its identity by checking whether  $H_1(I_{Di}, PW_i)$  equal to the stored value. If the verification fails, the TPD aborts it.
- The TPD of vehicle  $V_i$  randomly chooses a number  $r_i \in \mathbb{Z}_q$  to compute  $R_i = r_iP$  and its pseudo-identity  $PID_i = H_2(r_iP_{pub}, T_i) \oplus I_{Di}$ , where  $T_i$  denotes the current timestamp. Then, it uses its SSK  $s$  to compute  $k_i = r_i + s \cdot H_1(PID_i, T_i)$  and  $(R_i)_x$ , where  $(R_i)_x$  is the  $x$ -coordinate of point  $R_i$ . Finally, the TPD returns  $(PID_i, k_i, (R_i)_x, T_i)$  to vehicle  $V_i$ .
- On receiving  $(PID_i, k_i, (R_i)_x, T_i)$  from its TPD, the vehicle  $V_i$  randomly chooses  $u_i \in \mathbb{Z}_q$  to compute its one-time public key  $U_i = -u_iP$  and then computes the signature  $\delta_i = (\delta_{1i}, \delta_{2i})$  of the traffic emergency message  $m_i \in \{0, 1\}^n$ , where  $\delta_{1i} = ((R_i)_x \oplus (H_3(m_i) || (H_4(H_3(m_i)) \oplus m_i)))$ ,  $\delta_{2i} = k_i + u_i \cdot H_5(PID_i, T_i, \delta_{1i}, U_i)$ . Finally,  $V_i$  sends  $(PID_i, U_i, T_i, \delta_i)$  to the vehicles around it.

### C. Signature Verification Process

After receiving  $(PID_i, U_i, T_i, \delta_i)$ , to obtain the traffic emergency message  $m_i$  and verify its validity, a nearby vehicle  $V_j$  executes the following steps:

- First of all,  $V_j$  needs to verify the validity of the timestamp  $T_i$  by checking whether the relation  $|T_i - T_c| \leq T$  holds, where  $T_c$  denotes the current timestamp, and  $T$  denotes the allowed maximum transmission delay of the traffic emergency message. If it is not satisfied, the message received is rejected. Otherwise,  $V_j$  goes on to the next step.
- Next, to recover the  $R_i$ ,  $V_j$  computes the equation  $R_i = \delta_{2i} \cdot P + H_1(PID_i, T_i) \cdot P_{pub} + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot U_i = r_i P + H_1(PID_i, T_i) \cdot sP + H_1(PID_i, T_i) \cdot (-sP) + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot u_i P + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot (-u_i P) = r_i P$ . Then, it computes  $string = \delta_{1i} \oplus (R_i)_x$  and extracts message  $m_i$  by computing  $m_i = \text{Right}(string, n) \oplus H_4(\text{Left}(string, |q| - n))$ , where  $\text{Right}(str, x)$  and  $\text{Left}(str, x)$  denote the least significant  $x$  bits of  $str$  and the most significant  $x$  bits of  $str$ , respectively.
- Finally,  $V_j$  verifies whether the equation  $H_3(m_i) = \text{Left}(string, |q| - n)$  holds. If it holds, the signature  $\delta_i$  and message  $m_i$  are valid; otherwise,  $V_j$  rejects the message.

### III. PROPOSED REPLAY ATTACK ON WEI ET AL. SCHEME

Suppose  $X$  represents all valid messages a vehicle can generate ( $X = \{M_1, M_2, \dots, M_n\}$ ). Let adversary (Adv) capture a valid message  $M_v \in X$ . The replay attack window is represented by the interval  $W = \{T_i - T | T_i \in \text{timestamps}(X), T_c \in \text{current\_time}\}$ . The verification process might succeed if Adv replays the message within this window ( $T_c \in W$ ). Suppose two timestamps  $T_1$  and  $T_2$  such that  $T_1 < T_2$ . We will demonstrate how Adv can exploit the vulnerability in the Wei et al. scheme [1] to execute a replay attack. Adv captures a valid message at timestamp  $T_1$ , denoted as  $M_{T_1} = (PID_i, U_i, T_1, \delta_1)$ , where  $PID_i$ ,  $U_i$ , and  $\delta_1$  are the pseudo-identity, one-time public key, and signature respectively. The Adv replays  $M_{T_1}$  at timestamp  $T_2$ , forming a replayed message  $M_{T_2} = (PID_i, U_i, T_2, \delta_1)$ .

According to the Wei et al. scheme [1], the verification process checks the validity of the timestamp  $T_i$  by comparing it with the current timestamp  $T_c$ . The message is valid if  $|T_i - T_c| \leq T$  holds, where  $T$  is the maximum transmission delay. Since the replayed message  $M_{T_2}$  has a timestamp  $T_2$ , and the verification window  $T$  allows for messages within a certain time range,  $|T_2 - T_c| \leq T$ , the algorithm accepts  $M_{T_2}$  as a valid message. Accepting the replayed message  $M_{T_2}$  allows the Adv to disseminate false information or disrupt the normal operation of the VANET system without being detected.

To illustrate how vehicle  $V_j$  can accept the same message twice at timestamps  $T_1$  and  $T_2$  within the allowed maximum transmission delay  $T$ , we consider a scenario where a replay attack occurs. Let's assume that vehicle  $V_j$  receives the identical message  $M$  at timestamps  $T_1$  and  $T_2$ , where  $T_1 < T_2$ . This message  $M$  comprises the components  $(PID_i, U_i, T_i, \delta_i)$ .

Here's how  $V_j$  would accept the same message twice:

*Verification of Timestamps:*  $V_j$  verifies the validity of the timestamp  $T_i$  for both messages  $M_1$  and  $M_2$  by checking whether  $|T_i - T_c| \leq T$ , where  $T_c$  is the current timestamp

and  $T$  is the maximum transmission delay. If  $|T_1 - T_c| \leq T$  and  $|T_2 - T_c| \leq T$ ,  $V_j$  proceeds to the next step.

*Recovery of  $R_i$  and Message Extraction:*  $V_j$  computes  $R_i$  using the equation:

$$\begin{aligned} R_i &= \delta_{2i} \cdot P + H_1(PID_i, T_i) \cdot P_{pub} + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot U_i \\ &= r_i P + H_1(PID_i, T_i) \cdot sP + H_1(PID_i, T_i) \cdot (-sP) \\ &\quad + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot u_i P \\ &\quad + H_5(PID_i, T_i, \delta_{1i}, U_i) \cdot (-u_i P) = r_i P. \end{aligned}$$

After computing  $R_i$ ,  $V_j$  derives the string  $string = \delta_{1i} \oplus (R_i)_x$  and extracts the message  $m_i$  from it.

*Verification of Message Validity:*  $V_j$  verifies whether the equation  $H_3(m_i) = \text{Left}(string, |q| - n)$  holds. If the equation holds for both messages  $M_1$  and  $M_2$ ,  $V_j$  accepts both messages as valid.

In this scenario,  $V_j$  accepts both messages  $M_1$  and  $M_2$  because they fall within the allowed maximum transmission delay  $T$  and satisfy the message validity checks. This proves how the replay attack allows  $V_j$  to accept the same message multiple times at different timestamps.

*Discussion and solution:* While timestamps provide a basic level of freshness, they can still be vulnerable to replay attacks within a short window. We can combine timestamps with nonces for better protection.

During signature generation (step II.B), each vehicle  $V_i$  incorporates a random nonce ( $N_i$ ) alongside the timestamp ( $T_i$ ) in the message  $(m_i || T_i || N_i)$ . This nonce, unique for each message, adds an additional layer of randomness. The concatenated string  $(m_i || T_i || N_i)$  undergoes hashing using  $H_3$  before further signature generation. Subsequently,  $V_i$  transmits  $(PID_i, U_i, T_i, N_i, \delta_i)$  to other vehicles in the network.

During verification (step II.C), upon receiving  $(PID_i, U_i, T_i, N_i, \delta_i)$ , each vehicle  $V_j$  follows a process similar to Wei et al.'s scheme [1]. It verifies timestamps, recovers  $R_i$ , and extracts  $m_i$ . During message verification,  $V_j$  ensures that the equation  $H_3(m_i || T_i || N_i) = \text{Left}(string, |q| - n)$  holds. If this equation holds for both messages  $M_1$  and  $M_2$ ,  $V_j$  deems both messages as valid.

### IV. CONCLUSION

In our analysis of Wei et al.'s privacy-preserving authentication protocol in VANET, we have identified a major security flaw. Despite claims of being secure, the protocol is vulnerable to replay attacks. This means malicious vehicles can replay messages multiple times, leading to a DOS attack. Additionally, the identity of the malicious vehicle cannot be traced, making the protocol unreliable in ensuring authentication privacy.

### REFERENCES

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